

Multiline formulas

Publications Department of IMPAN

publ@impan.pl

<https://www.impan.pl/en/publishing-house/for-authors>

April 11, 2018

• *A general remark:* the constructs (“environments”) discussed below require the use of the `amsart` style or `\usepackage{amsmath}` and are of two types:

- (1) the `align`, `gather`, `multline` and `alignat` environments concern the whole equations, i.e. they replace `equation` (an exception: `align` can be used inside `gather`);
- (2) `split`, `aligned`, `gathered` and `alignedat` are “subsidiary environments”: they can only appear inside others, like `equation`, `align` or `gather`, and may embrace only some part of a displayed line.

Some constructs below require `\usepackage{mathtools}` or `\usepackage{enumitem}`.

• *A piece of advice:* forget `eqnarray`!

1 One multiline formula

• Quite often one formula (i.e. a sequence of expressions connected by binary operations and relations) takes more than one line. As a rule, one formula (in this sense) should have one number; numbering parts of it separately is seldom necessary. In case of need, you can refer to a specific line of a formula by writing e.g. $(1.1)_2$.

If equation numbers are placed on the left (as in the `amsart` style, and also in IMPAN journals), the number is normally on the first line of a multiline formula; if the numbers are on the right, it is on the last line. (Warning: this convention is followed by many publishers, but not all: sometimes the number is centred.)

• If there are no natural places for alignment, use `multline`:

$$(1.1) \quad \begin{aligned} & \text{aaaaaaaaaaaaaaaaaaaaaaaaaaaaa} \\ & \quad + \text{bbbbbbbbbbbbbbbbbbbbbbbbbbbbbb} \\ & \qquad \qquad \qquad \leq \text{ddddddddddddddddddddddddd} \end{aligned}$$

The first line is set (almost) flush left, the last line is (almost) flush right, and the middle lines (if any) are centred.

- You can shove any middle line within `multline` to the right or to the left by making it the argument of `\shoveright` or `\shoveleft`:

$$(1.2) \quad \begin{aligned} & aaaaaaaaaaaaaaaaaaaaaaaaaaaaaa \\ & + bbbbbbbbbbbbbbbbbbbbbbbbbbb + dddddddd \\ & \hspace{10em} \times eeeeeeeeeeeeeeeeeee \\ & \leq ddddddddddddddddddd. \end{aligned}$$

- You can align a group of lines within `multline`, using `aligned`:

$$(1.3) \quad \begin{aligned} & aaaaaaaaaaaaaaaaa + xxxxxxxxxxx \\ & \hspace{10em} < bbbbbbbbbbbbbbb \\ & \hspace{10em} + ddddddddddddddd \\ & \hspace{10em} < ccccccccccccccc. \end{aligned}$$

- To code an “object” consisting of centred lines within a formula, use `gathered`:

$$(1.4) \quad \text{Pascal}_4 = \begin{array}{c} 1 \\ 1 \ 2 \ 1 \\ 1 \ 3 \ 3 \ 1 \\ 1 \ 4 \ 6 \ 4 \ 1 \end{array}$$

If you want to bottom-align two such objects, apply `gathered[b]` (then you have to add `split` to centre the equation number):

$$(1.5) \quad \begin{array}{c} 1 \\ 1 \ 2 \ 1 \\ 1 \ 3 \ 3 \ 1 \end{array} \quad \begin{array}{c} 1 \\ 1 \ 2 \ 1 \\ 1 \ 3 \ 3 \ 1 \\ 1 \ 4 \ 6 \ 4 \ 1 \end{array}$$

With `gathered[t]`, you get top alignment:

$$\begin{array}{c} 1 \\ 1 \ 2 \ 1 \\ 1 \ 3 \ 3 \ 1 \end{array} \quad \begin{array}{c} 1 \\ 1 \ 2 \ 1 \\ 1 \ 3 \ 3 \ 1 \\ 1 \ 4 \ 6 \ 4 \ 1 \end{array}$$

- The `aligned[t]` and `aligned[b]` constructions enable independent and/or nested alignments, e.g., `aligned[t]` inside `aligned`:

$$(1.6) \quad \begin{aligned} A = xyz &= ztv + [f_1(a, b, c, d, e, f, g, h), \\ & \hspace{2em} f_2(a, b, c, d, e, f, g, h), \\ & \hspace{2em} f_3(a, b, c, d, e, f, g, h)] \\ & = ccccccccccc \end{aligned}$$

or `aligned[b]` inside `aligned`:

$$\begin{aligned} & xxxxxx + [f_1(a, b, c, d, e, f, g, h), \\ & \hspace{2em} f_2(a, b, c, d, e, f, g, h), \\ & \hspace{2em} f_3(a, b, c, d, e, f, g, h)] = ttttttttttttttttt \\ & = bbbbbbbbbbb. \end{aligned}$$

- To move a line within an aligned structure to the left or to the right, use `MoveEqLeft` with a positive or negative parameter (this requires `\usepackage{mathtools}`):

$$\begin{aligned}
 (1.7) \quad xxxx &= yyyyyyyyyyyyyy + [eee \\
 &\qquad\qquad\qquad \times zzzzzzzzzzzzzzzzzz] \\
 &= tttttttttttttttt \\
 &= vvvvvvvvvvvv.
 \end{aligned}$$

- If the formulas are left-numbered, you can also label a longer statement as a “formula”, by treating it as an item of an itemized list (this requires `\usepackage{enumitem}`; the “leftmargin” parameter has to be adjusted according to the width of the formula number):

- (1.8) Here you can place any statement, even taking several lines of text and including displayed formulas, like

$$aaaa = bbb.$$

- (1.9) Next item.

2 Several formulas or sets of displayed conditions

- Separate formulas should end with a comma or semicolon—to make it clear that the next line is not a continuation of the preceding one.
- If there are no natural places for vertical alignment, use `gather`:

$$(2.1) \quad aaaaaaaaa = b, \quad cc = xxx, \quad dd = yyy,$$

$$(2.2) \quad mmmmmmmmmmmmm = 0 \quad \text{for all } i = 1, \dots, n.$$

Note the spacing between parts of a formula on the same line; you can use `\quad` (small space), `\quad\quad` (medium space) or `\quad\quad\quad` (large space).

- If a formula number is unnecessary, you can “switch it off”, using `\notag`:

$$\begin{aligned}
 (2.3) \quad aaaaaaaaa &= b, \quad cc = xxx, \quad dd = yyy, \\
 mmmmmmmmmmmmm &= 0 \quad \text{for all } i = 1, \dots, n.
 \end{aligned}$$

(A formula number not cited in text is “information noise”; also, the number takes some space and often causes the formula to occupy one line more. As a rule, number only those formulas that are referred to later.)

- If no number is necessary, use `gather*`:

$$\begin{aligned}
 aaaaaaaaa &= b, \quad cc = xxx, \quad dd = yyy, \\
 mmmmmmmmmmmmm &= 0 \quad \text{for all } i = 1, \dots, n.
 \end{aligned}$$

- If you need one centred number (for a group of equations), instead of `gather` use `gathered` inside `equation`:

$$\begin{aligned}
 (2.4) \quad aaaaaaaaa &= b, \quad cc = xxx, \quad dd = yyy, \\
 mmmmmmmmmmmmm &= 0 \quad \text{for all } i = 1, \dots, n.
 \end{aligned}$$

- You can also “gather” several “multlines”, using the subsidiary construct `multlined`, available in `mathtools`, with optional parameters indicating the placement of formula numbers and the width of the formulas:

$$(2.5) \quad \begin{aligned} & aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa \\ & \quad + bbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbbb \\ & \hspace{15em} \times yyyyyyyyyyy \\ & = xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx, \end{aligned}$$

$$(2.6) \quad \begin{aligned} & cccccccccccccccccccccccccccccccccccc \\ & = ddddddddddddddddddddddddddddddddddd. \end{aligned}$$

- In most cases, however, we want to align something, and then we use `align`:

$$(2.7) \quad \begin{aligned} & xxxxx = yyyyyyyyyyyyyyy \\ & \quad + zzzzzzzzzzzzzzzzzzzz, \end{aligned}$$

$$(2.8) \quad bbb = tttttttttttttt,$$

$$(2.9) \quad hh = vvvvvvvvvv.$$

Note that the alignment symbols, called ampersands (&), should be placed **to the left** of binary relation signs; if, as above, part of an expression is continued on the next line, put `&\quad` before the binary operation sign.

Remember that you cannot place & signs anywhere: the parts between two & signs and between & and `\` should be “separate formulas” (in the \TeX sense), so you cannot e.g. put a & inside `{ }` or inside `\left-\right`.

- If you need one centred number for a group of aligned equations, use `split` or `aligned` inside `equation`:

$$(2.10) \quad \begin{aligned} & xxxxx = yyyyyyyyyyyyyyy \\ & \quad + zzzzzzzzzzzzzzzzzzzz, \\ & bbb = tttttttttttttt, \\ & hh = vvvvvvvvvv. \end{aligned}$$

- If you have two “split” sets of equations and you want them to have a common alignment, you have to use two `split`’s inside `align` (this is the advantage of `split` over `aligned`):

$$(2.11) \quad \begin{aligned} & aaaaaaaaaaaaaaaaaaaaaaaaaa = bbbbbbbbbbbb, \\ & \hspace{10em} bbbb = xxxxxx, \end{aligned}$$

$$(2.12) \quad \begin{aligned} & cccc = yyyyyyy, \\ & dddddd = zzzzz. \end{aligned}$$

If you do not want “aligned alignments”, use `split` or `aligned` inside `gather`:

$$(2.13) \quad \begin{aligned} & aaaaaaaaaaaaaaaaaaaaaaaaaa = bbbbbbbbbbbb, \\ & bbbbbbbbbbbbbbbbbbbbbbbb = xxxxxx, \end{aligned}$$

$$(2.14) \quad \begin{aligned} & cccc = yyyyyyy, \\ & dddddd = zzzzz. \end{aligned}$$

- If you need several aligned “columns”, you can still use `align` or `align*`, but you have to add additional ampersands separating the columns:

$$\begin{aligned} aa = bbbb, & \quad dd = ee & \text{(by Lemma 2),} \\ hh = ii, & \quad ll = kkkkk & \text{(by (2.14)).} \end{aligned}$$

However, here you do not control the spacing between the columns. If you want to prescribe it, use `alignat` (or `alignat*`), which has a parameter (the number of columns) and requires specifying the intercolumn spaces:

$$(2.15) \quad aa = bbbb, \quad dd = ee \quad (\text{by Lemma 2}),$$

$$(2.16) \quad hh = ii, \quad ll = kkkkkk \quad (\text{by (2.14)}).$$

• `alignat` also has a subsidiary version, `alignedat`, which you can put inside `equation` if you need one centred number:

$$(2.17) \quad aa = bbbb, \quad dd = ee \quad (\text{by Lemma 2}),$$

$$hh = ii, \quad ll = kkkkkk \quad (\text{by (2.14)}).$$

• If you want the consecutive equations of a group of equations to be numbered e.g. (2a), (2b) etc., use `subequations`, inside which you can place the previous constructs, e.g., `alignat` inside `subequations`:

$$(2.18a) \quad aa = bbbb, \quad dd = ee \quad (\text{by Lemma 2}),$$

$$(2.18b) \quad hh = ii, \quad ll = kkkkkk \quad (\text{by (2.14)}).$$

or `gather` inside `subequations`:

$$(2.19a) \quad \begin{aligned} &aaaaaaaaaaaaaaaaaaaaaaaa = bbbbbbbbbbbb, \\ &bbbbbbbbbbbbbbbbbbbbbb = xxxxxx, \end{aligned}$$

$$(2.19b) \quad \begin{aligned} &cccc = yyyyyyy, \\ &ddddddd = zzzzz. \end{aligned}$$

Note the independent labels of the whole group and its parts; writing `\eqref{E:suba}`, we invoke the whole system (2.18), while writing `\eqref{E:suba1}` we refer to (2.18a).

• If you want to place a longer comment in the middle of an aligned construction, you can use `\intertext` (this only works within `align` or `align*`, but not with `aligned`):

$$(2.20) \quad \begin{aligned} xxxxx = yyyyyyyyyyyyyy + [eee \\ \quad \quad \quad \times zzzzzzzzzzzzzzzzzz] \end{aligned}$$

(note that we have not used the full strength of (H) here, but only the concavity of f)

$$= tttttttttttttt$$

$$= vvvvvvvvvvv.$$

References

- [1] G. Grätzer, *More Math into L^AT_EX*, 4th ed., Springer, Berlin, 2007.